| Grade Level Proficiency Descriptors |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| Aspect | Sub-Aspect | K | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|  | Understands the realworld problem | Makes a personal connection with one aspect of the problem <br> personal connection experiences and prior knowledge | Makes personal connections with aspects of the problem <br> personal connection: experiences and prio knowledge | Makes persona connections to explore the problem <br> personal connection experiences and prio knowledge | Makes personal connection to explore the problem <br> personal connection knowledge | Makes general connections to understand the problem in context <br> general connection: personal or to similar problems | Makes general connections to understand the problem in context <br> general connection: personal or to simila problems | Makes relevant connections to understand a realworld problem <br> real-world problem: contextual, relevant, related to current learning, personally/locally/globally meaningful | Makes relevant connections to understand a realworld problem <br> real-world problem: contextual, relevant, related to current learning, <br> personally/locally/globally meaningful | Makes relevant connections to fully understand the real world problem in context <br> real-world problem: contextual, relevant, related to curr personally <br> meaningful | Makes relevant connections to fully understand the real world problem in context <br> real-world problem: contextual, relevant, related to curren learning, $\qquad$ meaningful | Makes connections necessary to understand the context and -implications of the real-world problem <br> real-world problem: contextual, relevant related to cur learning, personally/locally/globally meaningful | Makes connections necessary to investigate and understand new contexts and implications of realworld problems <br> real-world problem: contextual, relevant, learning, $\qquad$ <br> meaningful | Makes connections necessary to investigate and understand new contexts and implications of real world problems <br> real-world problem contextual, relevant related to current learning, <br> personally/locally/globally <br> meaningful |
| Interprets | Extracts relevant information | Identifies a significant fact about the problem | Identifies a significant fact and gathers other information from the problem | Identifies and gathers most of the significant information from the presented problem to assist in solving the problem | Identifies and gathers most of the significant information from the presented problem to assist in solving the problem | Gathers relevant information from the presented problem to assist in solving the problem <br> the problem | Gathers relevant information from the presented problem to assist in solving the problem | Extracts relevant information from the presented problem needed to solve the problem | Extracts relevant information from the presented problem needed to solve the problem | Extracts relevant information from the presented problem and other external required to solve the problem. | Extracts relevant information from the presented problem and other external resources as needed problem. | Extracts and organizes relevant information from the presented problem and other external resources as needed from a variety of sources to be used in solving the problem. | Extracts and organizes relevant information from the presented curated external resources as needed from a variety of sources to be used in solving the problem. | Extracts and organizes relevant information from the presented problem and other resources as needed from a variety of sources to be used in solving the problem. |
|  | Identifies parameters and limitations | Understands that problems have parameters <br> parameters: factors and conditions which define the problem | Identifies a clearly defined parameter needed to solve the problem <br> parameters: factors and conditions which define the problem | Identifies some of the clearly defined parameters needed to solve the problem parameters: factors and conditions which define the problem the problem | Identifies most of the clearly defined parameters needed to solve the problem parameters: factors and conditions which defin the problem | Identifies all clearly defined parameters needed to solve the problem <br> parameters: factors and conditions which define the problem | Identifies all clearly defined parameters needed to solve the problem <br> parameters: factors and conditions which define the problem | Identifies only relevant explicit parameters needed to solve the problem <br> parameters: factors and conditions which define the problem | Identifies only relevant explicit parameters needed to solve the problem <br> parameters: factors and conditions which define the problem <br> limitations: reasonable constraints in a real world problem or context | dentifies relevant explicit parameters and limitations needed to solve the problem <br> parameters: factors and conditions which define the problem <br> limitations: reasonable onstraints in a real world problem or contex | Identifies relevant explicit parameters and limitations needed to solve the problem <br> parameters: factors and conditions which define the problem <br> limitations: reasonable constraints in a real | Identifies relevant explicit parameters and infers implicit limitations needed to solve the problem <br> parameters: factors and conditions which define the problem $\qquad$ constraints in a real world problem or context | Identifies explicit and mplicit parameters and limitations needed to solve the problem <br> parameters: factors and conditions which define the problem <br> imitations: reasonable constraints in a real world problem or context | Identifies explicit and implicit parameters and limitations of the problem <br> parameters: factors and conditions which define the problem <br> limitations: reasonable constraints in a real worl problem or context |


|  | Translates scenario into a mathematical problem (Mathematizes) | Recognizes the mathematical competencies and content needed to content: link to math curriculum | Recognizes the mathematical competencies and content needed to solve the problem content: link to math curriculum | Identifies the mathematical competencies and content needed to solve the problem content: link to math curriculum | Identifies the mathematical competencies and content needed to sove the problem content: link to math curriculum | Applies the mathematical understanding needed to partially translate a mathematical problem mathematical understanding: link to math curriculum math curriculum | Applies the mathematica understanding needed to partially translate a mathematical problem mathematical understanding: link to math curriculum | Applies the mathematica understanding needed to translate a familiar scenario into a mathematical problem <br> mathematical understanding: link to $\qquad$ or modelled | Applies the mathematical understanding needed to translate a familiar scenario into a mathematical problem <br> mathematical understanding: link to math curriculum $\qquad$ or modelled | Applies the mathematical understanding needed to translate an unfamiliar scenario into a mathematical problem. <br> mathematical understanding: link to math curriculum math curriculum unfamiliar: previously | Applies the mathematical understanding needed to translate an unfamiliar scenario into a mathematical problem. <br> mathematical understanding: link to math curriculum unfamiliar: previously | Applies the mathematical understanding needed to translate an unfamiliar scenario into a mathematica problem. <br> mathematical understanding: link to unfamiliar: previously | Applies mathematical understanding needed to translate a complex unfamiliar scenario problem. <br> mathematical understanding: link to math curriculum unfamiliar: previously unseen or unmodelled unseen or unmodelled | Applies mathematical understanding needed to translate a complex, unfamiliar scenario into a mathematical problem. <br> mathematical understanding: link to math curriculum unfamiliar: previously unseen or unmodelled cen or unmodelled |
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| Applies | Represents the mathematical problem (Visualization) | Represents the mathematical problem using concrete materials and/or pictures | Represents the mathematical problem using concrete materials and diagrams | Represents the mathematical problem using concrete materials and diagrams | Represents the mathematical problem using concrete materials, diagrams, and/or some familiar equations <br> familiar: previously seen or modelled | Represents the mathematical problem using concrete materials, diagrams, and/or some familiar equations <br> familiar: previously seen odelled | Represents the mathematical problem using concrete materials, diagrams, and/or equations | Accurately represents the mathematical problem using a variety of models models: e.g., concrete materials, diagrams, equations | Accurately represents the mathematica problem using a variety of models <br> models: e.g., concrete materials, diagrams, equations | Clearly represents the mathematical problem by choosing an appropriate model(s) <br> clearly: immediately demonstrates student's understanding <br> appropriate: link to Math curriculum <br> models: e.g., concrete materials, diagrams, equations | Clearly represents the mathematical problem by choosing an appropriate model(s) <br> clearly: immediately demonstrates student's understanding appropriate: link to Math curriculum models: e.g., concrete materials, diagrams, equations | Clearly and accurately represents the problem by an effective model(s) <br> clearly: immediately demonstrates student's understanding <br> effective: chooses a model which best fits the student's understanding and ability and ability models: e.g., concrete materials, diagrams, equations | Clearly and accurately represents the problem in context by strategically choosing an effective model(s) <br> clearly: immediately demonstrates student's understanding <br> in context: the representation is appropriate to the problem or scenario $\qquad$ which best fits the student's understanding and ability models: e.g., concrete materials, diagrams, equations | Clearly and accurately represents the problem in context by strategically choosing an effective model(s) <br> clearly: immediately demonstrates student's understanding <br> in context: the representation is appropriate to the <br> problem or scenario <br> effective: chooses a model which best fits the and ability models: e.g., concrete materials, diagrams, equations |
|  | Develops a plan of approach | Experiments with problem solving using prior knowledge | Develops a <br> straightforward plan of approach using prior knowledge and and strategies | Develops a basic plan of approach using familiar mathematical tools and/or strategies basic: could be one step familiar: previously seen or modelled | Develops a basic plan of approach using familiar mathematical tools and/or strategies basic: could be one step familiar: previously seen or modelled | Develops a sequence of steps that applies familiar mathematical tools and/or strategies familiar: previously seen or modelled | Develops a logical sequence of steps that applies familiar mathematical tools and/or strategies <br> familiar: previously seen or modelled | Develops an organized and intentional sequence of steps that applies appropriate and/or strategies <br> appropriate: link to Math curriculum | Develops logical and organized plan that applies appropriate mathematical tools <br> plan: an intentional <br> sequence of steps with an <br> appropriate: link to Math curriculum <br> strategies: e.g., Using a ool [calculator], picture graph, equation | Uses mathematical reasoning to develop a plan that applies appropriate mathematical tools and/or strategies <br> plan: an intentional <br> sequence of steps with an end goal <br> appropriate: link to Math curriculum <br> strategies: e.g., Using a graph, equation | Uses mathematical reasoning to develop a logical and organized plan that applie mathematical tools and/or strategies <br> plan: an intentional <br> sequence of steps with an end goal <br> appropriate: link to Math curriculum <br> strategies: e.g., Using a graph, equation | Uses mathematical reasoning to develop a logical, organized, and effective plan that applies appropriate and/or strategies <br> plan: an intentional sequence of steps with an end goal <br> appropriate: link to Math curriculum <br> strategies: e.g., Using a tool [calculator], Social Studies/Science. evidence from text | Uses mathematical reasoning to develop a logical, organized, and effective multi-step appropriate mathematical tools and/or strategies <br> plan: an intentional sequence of steps with an end goal <br> appropriate: link to Math curriculum $\qquad$ tool [calculator], algorithm, picture, graph; Social Studies/Science: evidence from text | Uses mathematical reasoning to develop a logical, organized, and effective multi-step appropriate mathematical tools and/or strategies <br> plan: an intentiona sequence of steps with an end goal appropriate: link to Math curriculum strategies: e.g., Using a tool [calculator], algorithm, picture, graph; Social Studies/Science: evidence from text |



|  | Reflects on the reasonableness of solution in context | Identifies a reasonable solution in relation to the original problem/question | Identifies a reasonable solution in relation to the original problem/question | Reflects on the easonableness of a solution in relation to the origina problem/question | Reflects on the reasonableness of a solution in relation to the original problem/question | Reflects on the reasonableness of their solution in relation to the original problem/question | Reflects on the reasonableness of their solution in relation to the original problem/question problem/question | Reflects on the reasonableness of their solution within the context of the problem $\qquad$ rationality, practicality context of the problem: e.g., Social $\qquad$ from text; Arts: soliciting feedback | Reflects on the reasonableness of their solution within the context of the problem <br> reasonableness: <br> rationality, practicality <br> context of the problem: <br> e.g., Social <br> Studies/Science: evidence from text; Arts: soliciting <br> feedback | Reflects on the validity of their solution within the context of the problem <br> validity: accuracy in <br> context <br> context of the problem: <br> e.g., Social <br> Studies/Science: evidence <br> from text; Arts: soliciting feedback feedback | Reflects on the validity of their solution within the context of the problem <br> validity: accuracy in context <br> context of the problem: e.g., Social Studies/Science: evidence feedback | Reflects on the validity of solution identifying contextual factors that may affect their answer <br> validity: accuracy in <br> solution: e.g., lab results, map, product, model, etc. contextual factors: Social Studies/Science: evidence from text: Arts: soliciting feedback | Reflects on the validity and reliability of processes and solutions, describing how contextual factors may affect their answer <br> validity: accuracy in context <br> reliability: reproducibility of results <br> contextual factors: Social Studies/Science: evidence from text; Arts: soliciting feedback | Reflects on the validity and reliability of processes and solutions, describing how contextual factors may affect their answer <br> validity: accuracy in context context reliability: reproducibility of results contextual factors: Social Studies/Science: evidence from text; Arts: soliciting from text; Arts: soliciting feedback |
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| Analyzes | Evaluates alternative approaches | Identifies an alternative approach | Identifies an alternative approach | Explores an alternative approach | Explores alternative approaches | Compares and contrasts alternative approaches approaches: own approach, peer-, or teacher-driven approach | Compares and contrasts alternative approaches <br> approaches: own approach, peer-, or teacher-driven approach | Describes the benefits and limitations of alternative approaches <br> approaches: own approach, peer-, or teacher-driven approach | Describes the benefits and limitations of alternative approaches <br> approaches: own approach, peer-, or eacher-driven approach | Evaluates the benefits and limitations of alternative approaches <br> approaches: own approach, peer-, or eacher-driven approach | Evaluates the benefits and limitations of alternative approaches <br> approaches: own approach, peer-, or teacher-driven approach, based approaches | Evaluates efficiency and effectiveness of alternative approaches <br> approaches: own approach, peer-, or teacher-driven approach; based approaches | Evaluates efficiency and effectiveness of alternative approaches and evaluates possible improvements <br> approaches: own approach, peer, or teacher-driven, comparison to researchbased approaches | Evaluates efficiency and effectiveness of alternative approaches and evaluates possible improvements $\qquad$ approach, peer-, or teacher-driven approach; based approaches |
|  | Revises approach as needed | Experiments with a recommended alternative approach to solve the problem | Experiments with a recommended alternative approach to solve the problem | Selects an alternative approach to solve the problem | Selects an alternative approach to solve the problem | Identifies and experiments with an alternative approach | dentifies and experiments with an alternative approach | Refines approach using the benefits and imitations of alternative approaches <br> refines: improves through small changes | Refines approach using the benefits and limitations of alternative approaches refines: improves through small changes | Revises approach using the benefits and imitations of alternative approaches <br> revises: reflects and adjusts adjusts | Revises approach based on their evaluation of alternative approaches revises: reflects and adjusts | Revises approach using the benefits and limitations of alternative approaches to compare alternative solution(s) <br> revises: reflects and | Redesigns approach to improve efficiency of process or accuracy of solution. <br> redesigns: iteratively reflects and adjusts | Redesigns approach to improve efficiency of process or accuracy of solution. <br> redesigns: iteratively reflects and adjusts |


|  | Represents processes and solution | Represents problem solving process using numbers, pictures, and/or manipulatives | Represents problem solving process using words, numbers, pictures, symbols and/or manipulativ <br> and/or manipulatives | Represents problem solving process using familiar tools <br> familiar tools: e.g., manipulatives, symbols, graphic organizers, charts | Represents processes and solution by selecting and using reasonable tools reasonable tools: table, manipulative, graphic organizer, array, model, etc. | Represents processes and solution by selecting and using reasonable tools reasonable tools: model, chart, map, table, graph, chart, array etc. | Represents processes and solution by selecting and using reasonable tools reasonable tools: model, chart, map, table, graph, chart, array etc. | Represents full process and solution by selecting and using appropriate tools <br> appropriate tools: model, chart, map, table, graph, chart, array, etc. | Represents full process and solution by selecting and using appropriate tools appropriate tools: model, chart, map, table, graph, chart, array, equation etc. | Effectively represents full process and solution using appropriate presentations <br> effectively: student selects an appropriate number of steps <br> appropriate <br> presentations: e.g., equation, graph, model, map, table, array) | Effectively represents <br> full process and <br> solution using <br> appropriate <br> presentations <br> effectively: student selects <br> an appropriate number of <br> steps <br> appropriate <br> presentations: e.g., <br> equation, graph, model, <br> map, table, diagram) | Represents complex pr ocesses and solutions using a variety of presentations in a manner that is suitable to the context <br> presentations: e.g., bulleted explanation, equation, graph, mode map, table, diagram) | Represents complex pr ocesses and solutions. Chooses a suited for mos context and purpose context and audience. <br> Presentation: e.g.. proof, model, equation, graph, model, map, table, diagram |  |
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| Communicates | Explains the approach taken | Identifies one step of their problem-solving approach | Outlines their problem-solving approach | Outines their problem-solving approach using familiar mathematical language <br> familiar previousts seen mathematical langugage: link to math curriculum | Describes their problem-solving approach using familiar mathematical language <br> familiar: previously seen mathematical language: link to math curriculum | Describes their problem-solving approach using familiar mathematical language <br> familiar: previously seen or modelled mathematical language: link to math curriculum | Describes their problem-solving approach using familiar mathematical language <br> familiar: previously seen or modelled mathematical language: link to math curriculum | Accurately explains the approach used approach: e.g., process: making a model, tool: using an equation | Accurately explains the approach used approach: e.g., process: making a model, tool: calculator, strategy: using an equation | Accurately explains the approach used, identifying limitations and assumptions of the approach <br> approach: e.g., process: making a diagram, tool: calculator, strategy: using an equation an equation | Accurately explains the approach used, identifying limitations and assumptions of the approach <br> approach: e.g., process: making a diagram, tool: an equation | Accurately explains in detail the approach used, describing any limitations and assumptions of the approach $\qquad$ making a flowchart tool calculator, strategy: using a familiar algorithm or evidence from text | Accurately explains in detail the approach used, evaluating the effect of any assumptions or approach approach <br> approach: e.g., process: making a flowchart, tool: calculator, strategy: using an algorithm or evidence from text <br> evaluate: assess the implications | Accurately explains in detail the approach used, evaluating the effect of any assumptions or limitations of the approach <br> approach: e.g., process: making a flowchart, tool: calculator, strategy: using an algorithm or evidence from text evaluate: assess the implications |
|  | Defends decisions and assumptions | $\begin{aligned} & \text { Identifies one } \\ & \text { problemsolving } \\ & \text { decision } \end{aligned}$ | Outlines one problemsolving decision | Describes one problem-solving decision and a supporting reason | Describes their problem-solving decisions and supporting reasons | Explains their problem-solving decisions and supporting reasons | Explains their problem-solving decisions and supporting reasons | Presents a rationale for their problemsolving decisions and assumptions | Presents a rationale for their problemsolving decisions and assumptions | Presents a logical argument and justifies their decisions and assumptions | Presents a logical argument and justifies their decisions and assumptions | Presents a valid, logical argument to justify their decisions about the selected approach and assumptions, and describes the effect of these choices | Presents a valid, logical argument to justify their decisions about the selected approach used, evaluating assumptions and the effect of these choices evaluate: assess the mplications | Presents a valid, ogical argument to justify their decisions about the selected approach used, evaluating assumptions and the effect of these choices evaluate: assess the |

